Warm Up 9/9

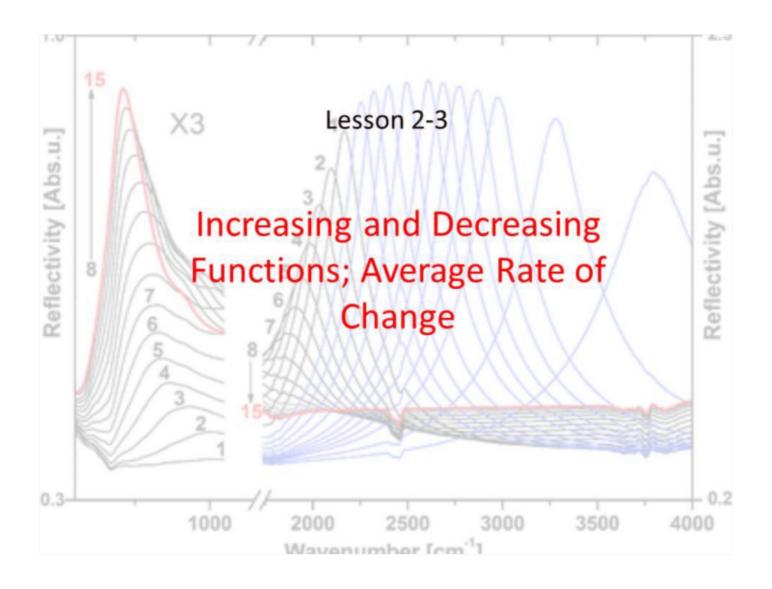
Find the slope of the line passing through the given points.

a.
$$(1,2)$$
, $(5,8)$

b. $(-1,3)$, $(0,2)$
 $M = \frac{4^2 - 4^2}{X_2 - X_1} = \frac{4^2 - 4^2}{X_1 - X_2}$
 $M = \frac{8^2 - 2}{5 - 1} = \frac{6}{4} = \frac{3}{2}$

c.
$$(0,0), (-11,7)$$

$$m = \frac{-7}{11}$$



Objective

Students will...

- Be able to determine whether a function is increasing or decreasing algebraically and using graphs.
- Be able to compute the average rate of change, and understand its relationship to the secant line.

Increasing and Decreasing Functions

<u>Functions</u> are often used to model changing quantities. Thus, it's important to see and analyze where a function is <u>increasing</u> or <u>decreasing</u>.

A function, say f is...

Increasing on an interval I if $f(x_1) < f(x_2)$ whenever $x_1 < x_2$ in I.

Decreasing on an interval I if $f(x_1) > f(x_2)$ whenever $x_1 < x_2$ in I.

In other words, when a bigger number is **inputted**, the **output** of an **increasing** function is greater, while the **output** of a decreasing function is smaller.

Examples

Determine whether the following functions are increasing or decreasing at the given interval.



a.
$$f(x) = x + 2$$
; [1,9]
 $f(1) = [+2 = 3]$
 $f(9) = 9 + 2 = []$

i Acreasing

$$g(-3) = \frac{3}{1+x^2}; [-3,0]; [1,5]$$

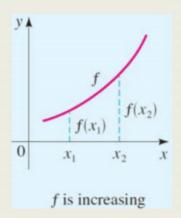
$$g(-3) = \frac{3}{1+x^2}; [-3,0]; [1,5]$$

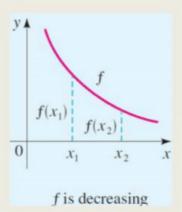
$$g(1) = \frac{3}{1+1} - \frac{3}{2} = \frac{3}{2}$$

$$g(5) - \frac{3}{1+25} = \frac{3}{2}$$

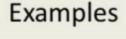
Graphs of Increasing and Decreasing Functions

Increasing and decreasing functions can also be easily seen graphically.

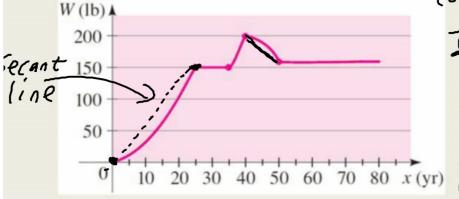




Thus, when viewing the graph from <u>left to right</u>, if the graph is rising the function is increasing, and vice-versa.



Determine the intervals on which the function W is increasing and on which it is decreasing, or neither. ((on s + an t),



Inc:[0,25].

[35,40].

20 30 40 50 60 70 80 x (yr) Dec: [40,50].

Warstont: [25,35]

[50,80]

Average Rate of Change

Sometimes it is important to find how much a graph has increased or decreased within a certain interval. One of the most useful ways to analyze such change is calculating the average rate of change.

the second average rate of change:
$$\frac{f(b)-f(a)}{b-a} = \frac{change in y}{change in x} = \frac{y_2-y_1}{x_2-x_1} = \mathcal{M}$$

As you can see the average rate of change is really the <u>slope</u> of the line connecting the <u>two endpoints</u> of a given interval. This line connecting the two endpoints is known as the <u>secant line</u>.

Examples

For the function $f(x) = (x - 3)^3$, find the average rate of

For the function
$$f(x) = (x-3)^3$$
, find the average rate of change between the following intervals:

a. $\begin{bmatrix} 1,3 \end{bmatrix}$

b. $\begin{bmatrix} 4,7 \end{bmatrix}$

a. $\begin{bmatrix} 1,3 \end{bmatrix}$

Comparison of the function $f(x) = (x-3)^3$, find the average rate of change between the interval $\begin{bmatrix} 2,7 \end{bmatrix}$.

Example

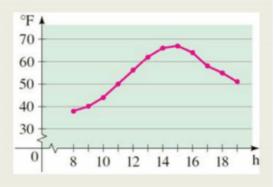
If an object is dropped from a tall building, then the distance it has fallen after t seconds is given by the function $d(t) = 16t^2$. Find its average speed (average rate of change) over the following intervals:

a.
$$t = 1$$
 s and $t = 5$ s b. $t = a$ and $t = a + h$

b.
$$t = a$$
 and $t = a + h$

Using the graph of the function of temperature F(t) in given time t, find the average rate of temperature between the following times:

- a. 8am to 9am
- b. 1pm to 3pm c. 4pm to 7pm



Homework 9/9

TB pg. #1-4, 13-23 (odd), 31