

$$(a+h)(a+h)$$

$$a^2 + ah + ah + h^2$$

### Warm Up 9/4

Let  $f(x) = 2x^2 + 3x - 1$ . Evaluate  $f(a)$ ,  $f(a+h)$ ,  $f = \frac{f(a+h) - f(a)}{h}$

$$f(a) = 2a^2 + 3a - 1$$

$$f(a+h) = 2(a+h)^2 + 3(a+h)$$

$$= 2(a^2 + 2ah + h^2) + 3a + 3h$$

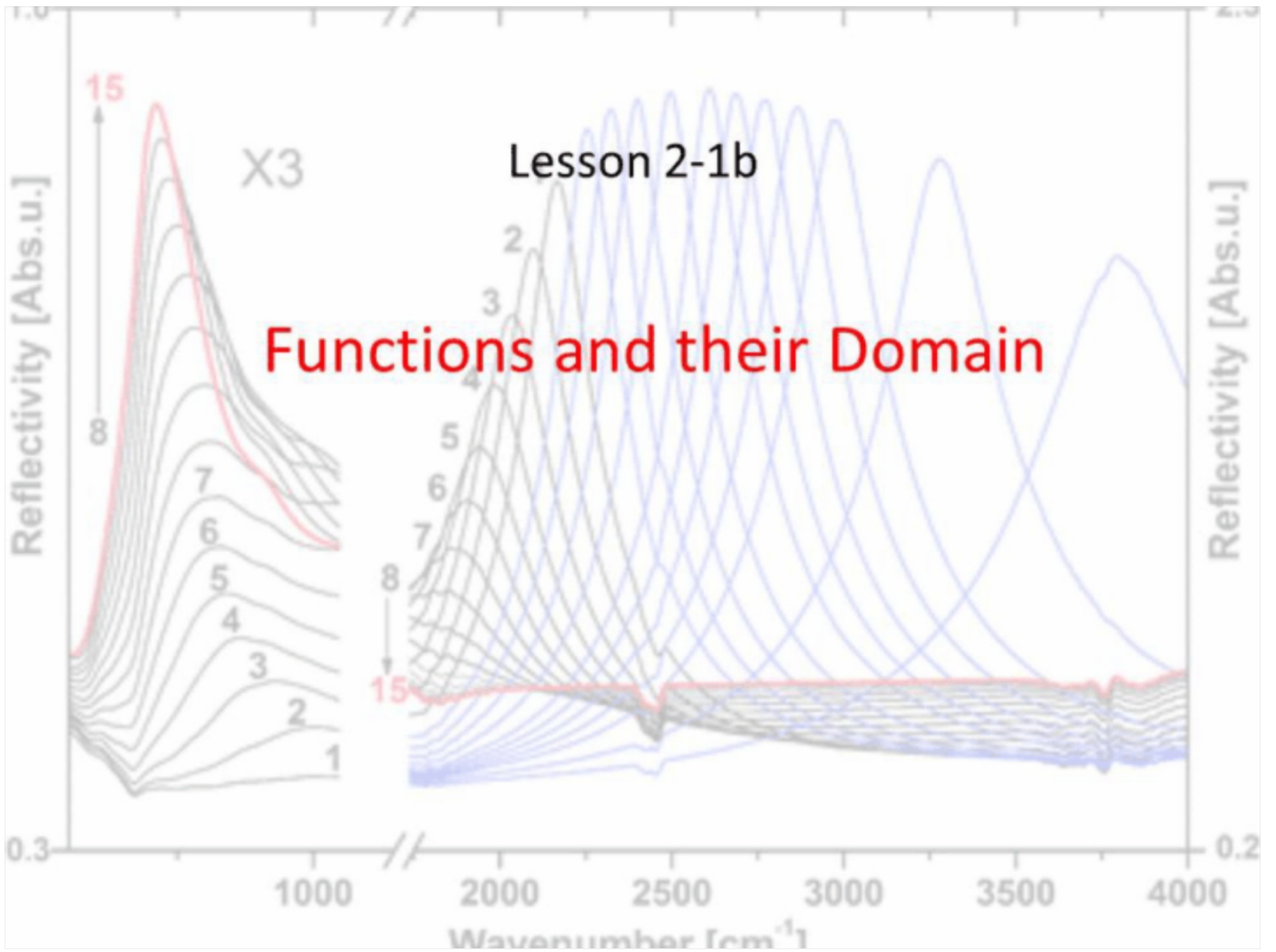
$$= 2a^2 + 4ah + 2h^2 + 3a + 3h$$

$$\frac{(2a^2 + 4ah + 2h^2 + 3a + 3h - 1) - (2a^2 + 3a - 1)}{h}$$

$$= \frac{4ah + 2h^2 + 3h}{h}$$

$$= \frac{h(4a + 2h + 3)}{h}$$

$$= 4a + 2h + 3$$



## Objective

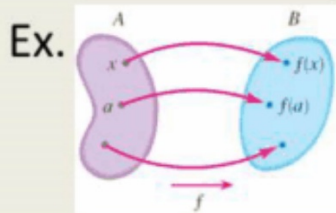
Students will...

- Be able to solve word problems using functional relationship.
- Be able to find the domains of functions.
- Be able to represent functions in multiple ways.

## Definition of a Function

So now we are ready to define what a function is.

A **function**, say  $f$ , is a rule that assigns to each element (item)  $x$  in a certain set  $A$  **exactly one** element, called  $f(x)$ , in a set  $B$ .



Another way to define function is for every **input**, there is exactly **one output**.

The set  $A$  is also known as the **domain**, and set  $B$  is known as the **range**.

## Word Problems Using Functions

If an astronaut weighs 130 pounds on the surface of the earth, then her weight when she is  $h$  miles above the earth is given by

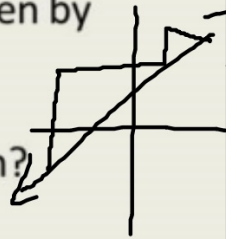
$$\text{the function: } w(h) = 130 \left( \frac{3960}{3960+h} \right)^2$$

a. What is her weight when she is 100 mi above the earth?

$$w(100) = 130 \left( \frac{3960}{3960+100} \right)^2 \approx 124$$

b. Construct a table of values of the function  $w$  that gives her weight at heights from 0 to 500 mi. What do you conclude from the table?

$h$	$w(h)$
0	
100	
200	
300	
400	
500	



## Word Problems Using Functions

If the speed limit on a 100-mile stretch of road is 75 miles per hour, then the amount of time it takes a car going  $x$  miles per hour over the limit to travel the stretch is given by  $f(x) = \frac{100}{75+x}$

- a. How long does it take the car to travel the stretch if the car is going 10 miles per hour over the limit?

$$f(10) = \frac{100}{85} = 1\frac{3}{17}$$

- b. How long does it take the car to travel the stretch if the car is not speeding at all?

$$f(0) = \frac{100}{75+0} = 1\frac{1}{3} \text{ hr.} \approx 1.3 = \text{80 min.}$$

## Domain of a Function

Recall that the **domain** of a function is the set of all **inputs**. Domain may be written **explicitly**. For example, for the function  $f(x) = x^2$ ,  $0 \leq x \leq 5$ , the domain is specifically set as all inputs between and including 0 and 5. Hence its domain is simply  $[0, 5]$ .

Whenever we have a function without the domain stated explicitly, we need to figure it out by algebraic reasoning.

Ex.  $f(x) = x^2 + 1$        $g(x) = \frac{1}{x-4}$        $h(x) = \sqrt{x}$

$(-\infty, \infty)$        $x \neq 4$   
 $(-\infty, 4) \cup (4, \infty)$        $x \geq 0$   
 $[0, \infty)$

$$x^2 - x = 0$$

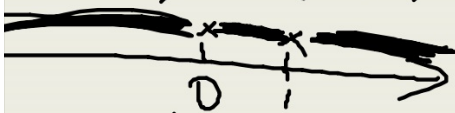
$$(x-1) = 0 \quad x = 0, 1$$

Examples

Find the domain of each function.

a.  $f(x) = \frac{1}{x^2 - x}$

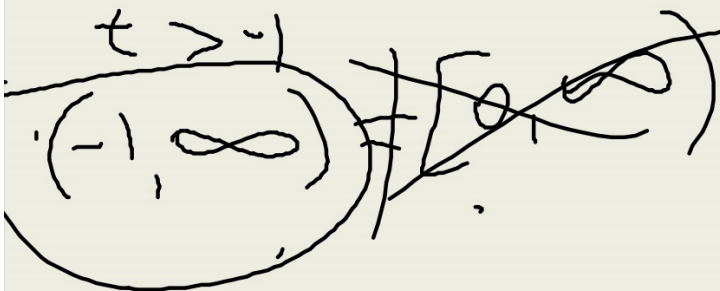
$$(-\infty, 0) \cup (0, 1) \cup (1, \infty)$$



c.  $h(t) = \frac{t}{\sqrt{t+1}}$

$$t+1 > 0$$

$$t > -1$$



$$9 - x^2 \geq 0$$

$$\pm \sqrt{9} \geq x$$

b.  $g(x) = \sqrt{9 - x^2}$

$$3 \geq x$$

$$-3 \leq x$$

$$-3 \leq x \leq 3$$

$$[-3, 3]$$



## Four Ways of Representing a Function

To help us understand what a function is, we have used machine and arrow diagrams. We can represent a functional relationship in following ways:

1. Verbally (by a description in words)

2. Algebraically (by an explicit formula)

$$f(x) = x^2$$

3. Visually (by a graph)



4. Numerically (by a table of values)

$x$	$f(x)$

# Four Ways to Represent a Function

## Four Ways to Represent a Function

### Verbal

Using words:

$P(t)$  is "the population of the world at time  $t$ "

Relation of population  $P$  and time  $t$

### Algebraic

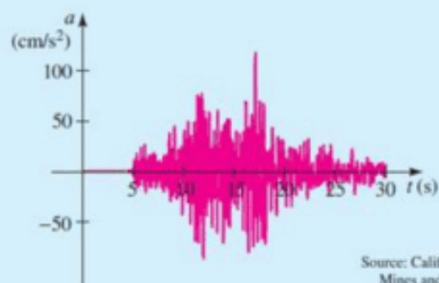
Using a formula:

$$A(r) = \pi r^2$$

Area of a circle

### Visual

Using a graph:



Source: Calif. Dept. of  
Mines and Geology

Vertical acceleration during an earthquake

### Numerical

Using a table of values:

$w$ (ounces)	$C(w)$ (dollars)
$0 < w \leq 1$	0.37
$1 < w \leq 2$	0.60
$2 < w \leq 3$	0.83
$3 < w \leq 4$	1.06
$4 < w \leq 5$	1.29
$\vdots$	$\vdots$

Cost of mailing a first-class letter

## Homework 9/4

TB pg. 156 #34, 38, 42, 44, 50, 58, 59, 66