

## Warm Up 1/07

No calculators allowed.

1.  $\sin \frac{4\pi}{3} = -\frac{\sqrt{3}}{2}$

$\frac{4}{3} > 1$   $\frac{4}{3} = 1 + \frac{1}{3} < \frac{1}{2}$

2.  $\cos \frac{3\pi}{4} = -\frac{\sqrt{2}}{2}$

$\frac{3}{4} < 1$

$\frac{3}{4} = \left(-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$

3. What does it mean for a function to have a period of  $\frac{3\pi}{4}$ ?

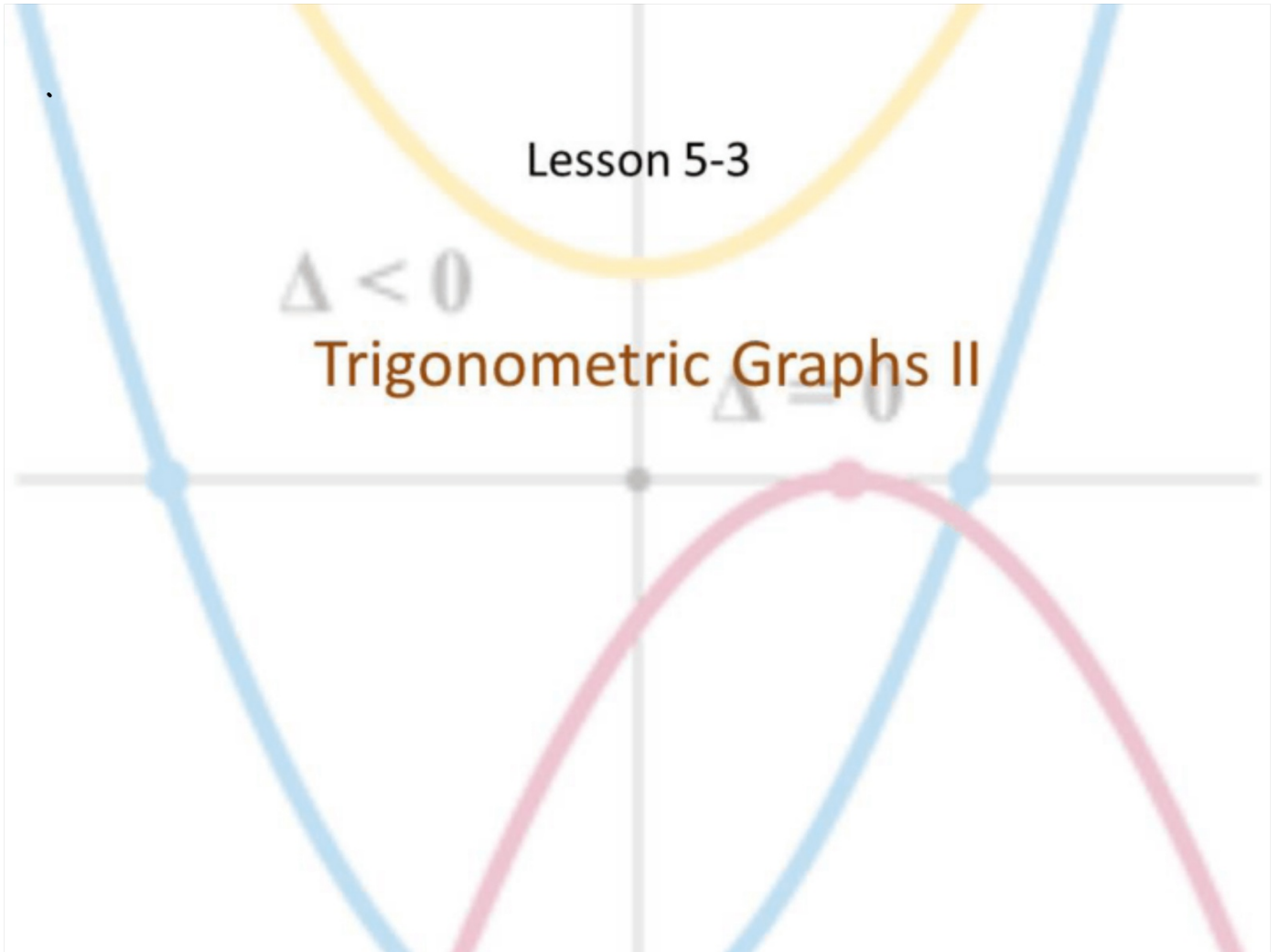
length of  
the cycle  
is  $\frac{3\pi}{4}$

Lesson 5-3

$\Delta < 0$

Trigonometric Graphs II

$\Delta = 0$



## Objective

Students will...

- Be able to know what the standard equation of a sine and a cosine curve is.
- Be able to find the period and the amplitude of a sine or a cosine function algebraically.

## Periodic Behavior of sin and cos

Before we can graph sin and cos functions, we need to take a closer look at their behavior.

One common behavior that we can quickly spot for any trigonometric function is the **repetition** of the values.

Ex:  $\sin 0 = 0 = \sin 2\pi, \sin \frac{\pi}{2} = 1 = \sin \frac{5\pi}{2}, \text{ etc.}$

$$\cos 0 = 1 = \cos 2\pi, \cos \frac{\pi}{2} = 0 = \cos \frac{5\pi}{2}, \text{ etc.}$$

For this reason, sin and cos functions are said to be **periodic**. This is why the unit circle is perfect for representing their values, because every circle is periodic (i.e. comes back to its starting point).

## Standard Equation of Sine and Cosine Curves

Like any other functions, there exists a standard equation of both sine and cosine curves.

$$y = 3 \cos^4 x \quad \cdot \quad \begin{array}{l} a = 3 \\ k = 4 \end{array}$$

**Sine Curves**: Any equation of a sine curve is written in the form:

$$y = a \sin kx, \text{ where } a \text{ and } k \text{ are real numbers with } k > 0$$

**Cosine Curves**: Any equation of a cosine curve is written in the form:

$$y = a \cos kx, \text{ where } a \text{ and } k \text{ are real numbers with } k > 0$$

$$\begin{array}{l} y = \pi \cos 3\pi x \\ a = \pi \\ k = 3\pi \end{array} \cdot$$

## Period and Amplitude of Sine and Cosine Curves

In our previous lesson we simply used the graph to figure out the period and amplitude of a given sine or cosine curve. However, we may not (more of than not) have a graph to refer to. In fact, how would we find the period if we were asked to graph a given sine or cosine curve? Of course, we can use the x-y table to graph the curve first, but this isn't always practical.

Fortunately, finding the period and the amplitude of a sine or cosine curve can be found algebraically from their equation.

For sine and cosine curves:  $y = a \sin kx$  and  $y = a \cos kx$ ,

$$y = \sin t \quad y = \cos t$$

$$\text{Period} = \frac{2\pi}{k}$$

$$\text{Amplitude} = |a|$$

## Examples

Find the period and amplitude of each function.

$$a = 4$$
$$k = 3$$

1.  $y = 4 \cos 3x$

$$\text{Per: } \frac{2\pi}{k} = \boxed{\frac{2\pi}{3}}$$

$$\text{Amp: } |a| = |4| = \boxed{4}$$

3.  $y = 2 \cos 3x$

$$\text{Per: } \boxed{\frac{2\pi}{3}}$$

$$\text{Amp: } 2$$

$$a = -2$$

$$k = \frac{1}{2}$$

2.  $y = -2 \sin \frac{1}{2}x$

$$\text{Per: } \frac{2\pi}{\frac{1}{2}} = 2\pi \cdot 2 = \boxed{4\pi}$$

$$\text{Amp: } |-2| = \boxed{2}$$

$$\frac{2}{4} = \frac{1}{2}$$

4.  $y = \pi \sin 4x$

$$\text{Per: } \frac{\pi}{2}$$

$$\text{Amp: } |\pi| = \pi$$

## Homework 1/07

TB pg. 429 #15-24 (ONLY FIND PERIOD AND AMPLITUDE) **DO NOT GRAPH!**