

Warm Up 9/5

Lesson 2-2: Graphs of Functions

Objective

Students will...

- Be able to make a table of values for a given function.
- Be able to graph each function using its table of values.
- Be able to determine the domain and the range of each function from its graph.

Four Ways of Representing a Function

To help us understand what a function is, we have used machine and arrow diagrams. We can represent a functional relationship in following ways:

1. _____ (by a description in words)
2. _____ (by an explicit formula)
3. _____ (by a graph)
4. _____ (by a table of values)

Four Ways to Represent a Function															
<p>Verbal</p> <p>Using words:</p> <p>$P(t)$ is "the population of the world at time t"</p> <p>Relation of population P and time t</p>	<p>Algebraic</p> <p>Using a formula:</p> <p style="text-align: right;">$A(r) = \pi r^2$</p> <p>Area of a circle</p>														
<p>Visual</p> <p>Using a graph:</p> <p style="text-align: right; font-size: small;">Source: Calif. Dept. of Mines and Geology</p> <p>Vertical acceleration during an earthquake</p>	<p>Numerical</p> <p>Using a table of values:</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>w (ounces)</th> <th>$C(w)$ (dollars)</th> </tr> </thead> <tbody> <tr><td>$0 < w \leq 1$</td><td>0.37</td></tr> <tr><td>$1 < w \leq 2$</td><td>0.60</td></tr> <tr><td>$2 < w \leq 3$</td><td>0.83</td></tr> <tr><td>$3 < w \leq 4$</td><td>1.06</td></tr> <tr><td>$4 < w \leq 5$</td><td>1.29</td></tr> <tr><td>\vdots</td><td>\vdots</td></tr> </tbody> </table> <p>Cost of mailing a first-class letter</p>	w (ounces)	$C(w)$ (dollars)	$0 < w \leq 1$	0.37	$1 < w \leq 2$	0.60	$2 < w \leq 3$	0.83	$3 < w \leq 4$	1.06	$4 < w \leq 5$	1.29	\vdots	\vdots
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Functions and their Graphs

If f is a function with domain A , then the graph of f is the set of ordered pairs: { _____ }

In other words, the graph of f is the set of all points (x, y) such that $y = f(x)$; that is, the graph of f is the graph of the equation $y = f(x)$.

Hence, we can place each input and output as an ordered pair, namely, (_____, _____).

Table of Values

Thus, we can graph every function the way we first learned how to graph- by making a table of values. Consider the following functions:

$f(x) = x^2$

$g(x) = x^3$

$h(x) = \sqrt{x}$

Graphing Functions

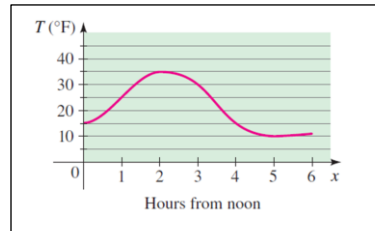
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Getting Information from the Graph

The values of a function are represented by the y -coordinates of its graph. So, we can read off the values of a function from its graph.

Ex. The function T graphed gives the temperature between noon and 6 P.M. at a certain weather station.

a. Find $T(1)$, $T(3)$, $T(5)$.



b. Which is larger, $T(2)$ or $T(4)$?

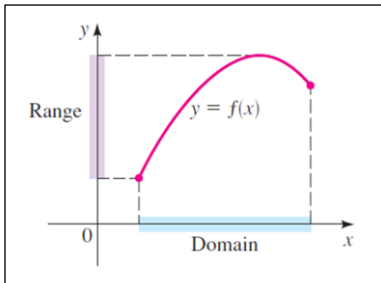
Domain and Range from Graphs

You can also determine the _____ and the _____ of functions from their graphs.

Remember that domain is all possible x -values, while the range is the all possible y -values. So, from the graph the domain is always from the lowest _____ to the highest _____.

Likewise, the range is from the **lowest y -coordinates** to the highest **y -coordinates**.

Ex.



Vertical Line Test

Remember that in a function, for every input there is exactly one output. Graphically this means that for every x -value there must be only one y -value. Thus, a _____ **test** can be used on a graph of any given expression to determine whether it is a function.

Vertical Line Test- A curve in the coordinate plane is the graph of a function if and only if no vertical line intersects the curve **more than** _____.

Ex.

