

Sequences/Limits.

Sequence - An array of numbers (finite or infinite)

ex. 1, 2, 3, 4, 5, ... infinite

1, 2, 3, 4, 5, ..., ||| finite

" a_n "

ex. $a_2 = 2^{\text{nd}}$ term

$a_3 = 3^{\text{rd}}$ term

$a_n = n^{\text{th}}$ term.

Arithmetic/Geometric

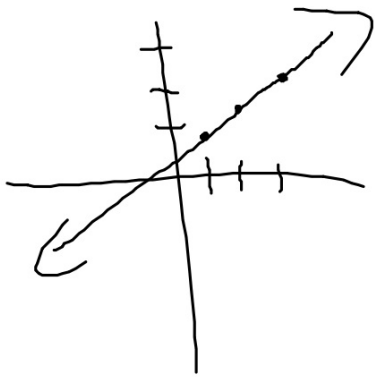
($i, \sqrt{2}, \pi, e, 3, -4$)

$$y = mx + b$$

Arithmetic Sequence - A sequence with a common difference, namely, adding or subtracting each time.
(Linear)

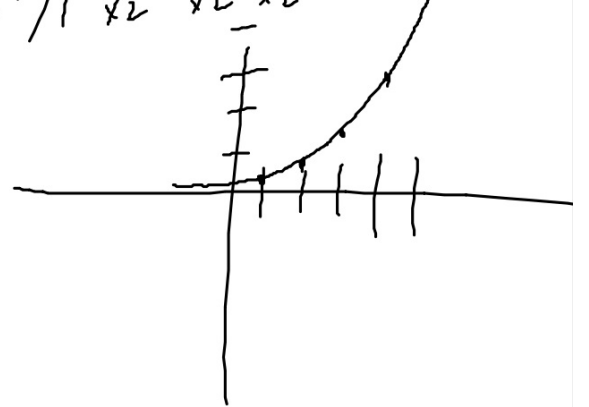
(Exponential) $y = a^x$
Geometric Sequence - A sequence with a common ratio, namely, multiplying each time.

x-coord.	n	1	2	3	4	5	6	...
ex. f(n)		1	2	3	4	5	6	...
y-coord.		1	2	3	4	5	6	...



x-coord.	n	1	2	3	4	5	6	...
ex. f(n)		$\frac{1}{4}$	$\frac{1}{2}$	1	2	4	8	...
y-coord.		$\frac{1}{4}$	$\frac{1}{2}$	1	2	4	8	...

$\times 2 \quad \times 2 \quad \times 2$



Explicit "formulas"

Arithmetic - $f(x) = mx + b$ ← movement.
 (common diff.)

ex. $-3, 0, 3, 6, 9, 12, 15, \dots$
 $+3 \quad +3$

$f(n) = 3n - 6$

ex. $0, 2, 4, 6, 8, \dots$
 $+2 \quad +2$

$f(n) = 1.2n - 1$

$-3^2 \neq 9$

Geometric - $f(x) = a^x$

1 2 3 4 ...
 ex. 4, 8, 16, 32, ...
 $\times 2 \times 2 \times 2 \dots$
 $a \rightarrow$

~~$f(x) = 2(2^x)$~~

$= 2^{x+1}$
 ex. $-12, 36, -108, \dots$

~~$f(x) = 4(3^x)$~~
 $f(1) = 4(-3^1) = -12$
 $f(2) = 4(-3^2) = -36$
 $f(x) = 4(-3)^x$
 $= (-1)^x 4(3)^x$

Sequences and Series,

Sequence - An array of numbers (finite or infinite).

ex, 1, 2, 3, 4, 5, 6, ..., 125 (finite)

1, 2, 3, 4, 5, 6, ... (infinite)

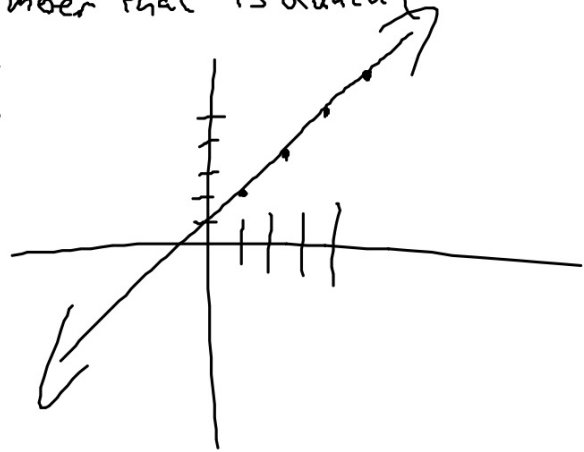
(Linear)

Arithmetic Sequence - A sequence with a common difference, named

" a_n " the number that is added (or subtracted) each time

$a_3 = 3^{\text{rd}}$ term
 $f(3) = 3^{\text{rd}}$ term

n	1	2	3	4	5	...
ex $f(n)$	2	3	4	5	6	...
x -coord.						
y -coord.		+1	+1	+1		



Explicit formula.

$f(x) = mx + b \Rightarrow$ arithmetic
common difference \rightarrow movement

ex. $-2, 5, 12, 19, 26, \dots$
 $+7 \quad +7 \quad +7$

$f(n)$

$$f(n) = 7n - 9$$

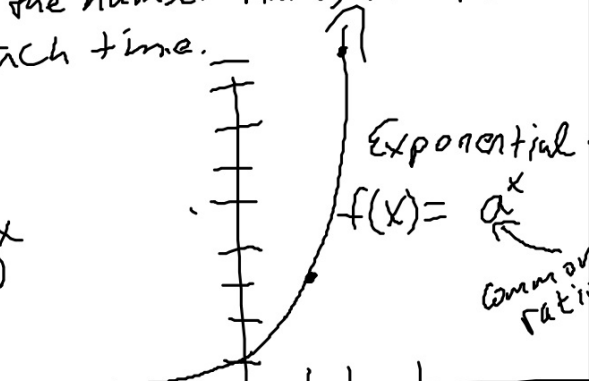
ex. $0.2, 1.4, 2.6, 3.8, 5.0, \dots$
 $+1.2 \quad +1.2 \quad + \dots$

$$f(n) = 1.2n - 1$$

Geometric Sequence - A sequence that has a common ratio, namely, the number that is multiplied (or divided) each time.

n	1	2	3	4
ex. f(n)	3	9	27	81
		$\times 3$	$\times 3$	$\times 3$

$$a^x = (a)^x$$



Explicit formula

$$f(x) = c a^x$$

factor of change \rightarrow c a \leftarrow common ratio

ex. $\frac{1}{4}, \frac{1}{2}, 1, 2, 4, 8, 16, \dots$

$\times 2 \quad \times 2 \quad \times 2 \quad \dots$

$$f(x) = \frac{1}{8}(2^x)$$

~~$$f(x) = \frac{1}{4}(2^x)$$~~

P E M D A S

ex. ¹-4, ²16, ³-64, ⁴256

$$f(x) = (-4)^x \quad \neq \quad -4^x$$

$$f(x) = (-1)^x 4^x$$

Sequences / Series

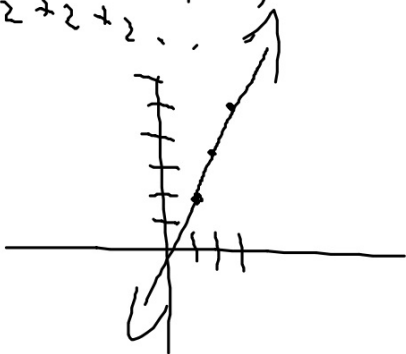
Sequence - An array of numbers (finite or infinite)

ex. 1, 2, 3, 4, ..., 11654 (finite)

ex. 1, 2, 3, 4, ... (infinite)

Arithmetic Sequence - A sequence that has a common difference
 Namely, the number that is added (or subtracted) each time.

x-Coord	n	1	2	3	4	5	6	...
y-Coord	f(n)	2	4	6	8	10	12	...
			+2	+2	+2	...		



"

Explicit Formula

ex. 0.3, 1.6, 2.9, 4.2, ...
+1.3 +1.3 +1.3 ...

$f(x) = mx + b$ ← movement
Common difference ↗

$$f(x) = 1.3x - 1$$
$$f(1) = 1.3 - 1 = 0.3$$

ex.

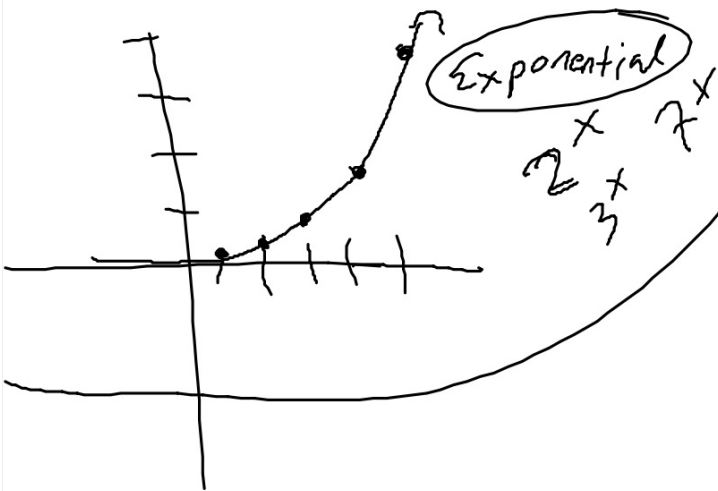
-2, 6, 14, 22, 30, ...
+8 +8 +8 ...

$$f(x) = 8x - 10$$

Geometric Sequence - A sequence that has a common ratio, namely, the number that is multiplied (or divided) each time.

ex.

n	1	2	3	each time
f(n)	$\frac{1}{4}$	$\frac{1}{2}$	1	2, 4, 8, ...
		$\times 2$	$\times 2$	$\times 2$...



Explicit Formula

$$f(x) = C a^x$$

factor of change \rightarrow a^x \uparrow common ratio

From ex.

$$f(x) = \left(\frac{1}{2}\right) 2^x$$

$$f(x) = 2^x \cdot \frac{1}{2}$$

$$f(1) = 2 \cdot \frac{1}{2}$$

$$= \frac{1}{2}$$

~~$$f(x) = 3(2^x) = 6^x$$

$$(a^x) \neq (ca)^x$$~~

ex. $-2, 6, -18, 54, -162, \dots$

$$\cancel{f(x) = \frac{2}{3}(-3^x)}$$

$$\cancel{= \left(\frac{2}{3}\right) \cdot 3^x}$$

$$f(x) = \frac{2}{3}(-3)^x$$

alternating

$$= (-1)^x \frac{2}{3}(3)^x$$

$$= f(1) = \frac{2}{3}(-3^1)$$

$$= -2 = a$$

$$f(2) = \frac{2}{3}(-3^2)$$

$$= -6$$