

Objective

Students will...

- Be able to know the geometric definition of a hyperbola.
- Be able to know and use the standard equation of hyperbolas and sketch their graphs.

Hyperbolas within a Cone

A hyperbola can be cut out from a cone.



Hyperbola

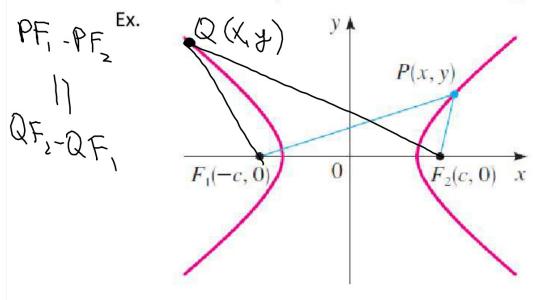


The shape of a cooling tower is a hyperbola.

Hyperbola

Here, we want to geometrically define what a hyperbola is.

<u>Geometric Definition of a hyperbola</u>- Is the set of all points in the plane, the difference of whose distances from two fixed points F_1 and F_2 is a constant. These two fixed points are the **foci** of the hyperbola.



Equations and Graphs of Hyperbolas

Using the distance formula, we can see that parabolas have the following equations: for a > 0 and b > 0 (not a > b)

Horizontal

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

Vertices: $(\pm a, 0)$

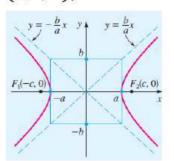
Covertices: $(0, \pm b)$

Transverse Axis: Horizontal length 2a



Asymptotes: $y = \pm \frac{b}{a}x$

Foci: $(\pm c, 0)$, $c^2 = a^2 + b^2$



Vertical

$$\frac{y^2}{a^2} - \frac{x^2}{b^2} = 1$$

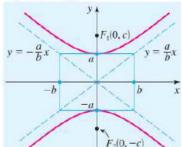
$$(0,\pm a)$$

$$(\pm b,0)$$

Vertical length 2a

$$y = \pm \frac{a}{b}x$$

$$(0, \pm c), c^2 = a^2 + b^2$$

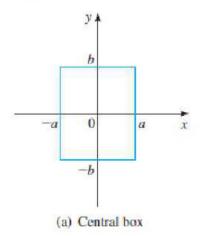


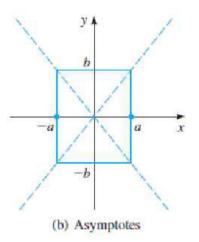
Sketching the Hyperbola

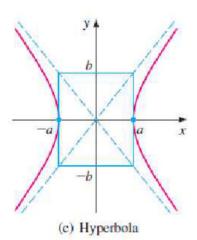
Here is a guidelines you can use to graph the hyperbola.

- 1. Sketch the central box, using the vertices and the covertices.
- 2. Sketch the asymptotes. These are the diagonals of the central box.
- 3. Plot the foci
- 4. Sketch the hyperbola.

Ex.

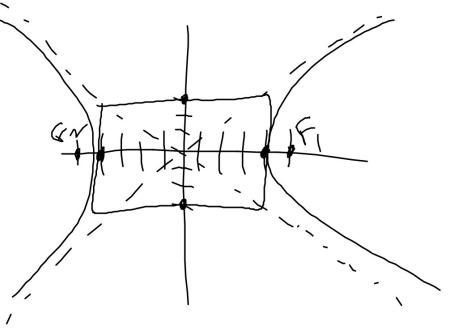






horiz.

$$\frac{9x^2 - 16y^2 = 144}{144} = \frac{144}{144} =$$



Vert.

$$x^{2} - 9y^{2} + 9 = 0 = 7 \times^{2} - 4y^{2} - 14y^{2}$$

$$= 7 y^{2} - 4y^{2} - 1$$

$$= 7 y^{2} -$$

$$\frac{y^2}{4} - \frac{x^2}{1} = 1$$

Homework 4/10

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