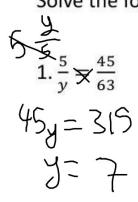
# Warm Up 1/26

Solve the following proportions.



$$2.\frac{2y}{9} = \frac{8}{4y}$$

$$3. \frac{2}{x-3} = \frac{8}{3x-3}$$





# Objective

#### Students will...

- Be able to know what Law of Sines is.
- Be able to apply the Law of Sines to solve for missing sides or angles.

#### Triangles

We've been studying the trigonometric ratios involving right triangles. Trigonometry can also be used for **non**-right triangles. First thing we need to do is to be consistent with our notations.

Consider the triangle  $\triangle ABC$  shown on the right.

The uppercase letters A, B, C represent the <u>vertices</u>,

or the <u>angles</u> of the triangle, while the lower case letters a, b, c represent the sides. For ease, the angles will always be labeled by uppercase letters, while the side <u>opposite</u> to each angle, will always be labeled with the lowercase letter of the opposite angle.

So, from our picture, we see that a is the side opposite to A, while b is the side opposite to B and c is the side opposite to C.

#### Law of Sines

There exists and important law regarding triangles (not just right triangles) derived from its **area formula**.

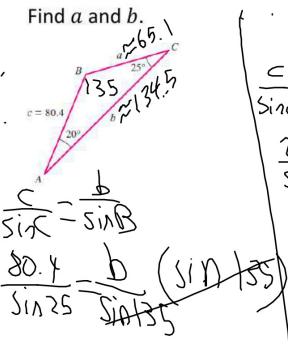
<u>Law of Sines</u>- For any triangle the lengths of its sides are proportional to the sines of the corresponding opposite angles. Namely, for  $\triangle ABC$ :

$$\frac{\Delta}{\sin A} = \frac{\sin A}{\sin B} = \frac{\sin C}{c}$$

#### Example

So we can apply the Law of Sines to solve for missing sides or angles.

(Important: Make sure your calculator is in the right mode!)



$$\frac{22}{\sin 63} - \frac{b}{\sin 75}$$

#### **Ambiguous Cases: Two solutions**

The two previous examples had <u>two</u> known angles. There may be a case where we might only have <u>one</u> known angle, but with two known sides. In either case, Law of Sines can be applied to solve the triangle. However, one important thing to bear mind here is the fact there may be more than one, or even <u>no</u> correct answer when the Law of Sines is applied with <u>one</u> known <u>angle</u> and <u>two</u> known <u>sides</u>. Consider the following: Solve triangle  $\triangle ABC$  if  $\angle A = 43.1^{\circ}$ ,  $\alpha = 186.2$ , and b = 248.6

Following: Solve triangle 
$$\triangle ABC$$
 if  $\angle A = 43.1^{\circ}$ ,  $a = 186.2$ , and  $b = 248.6$ 

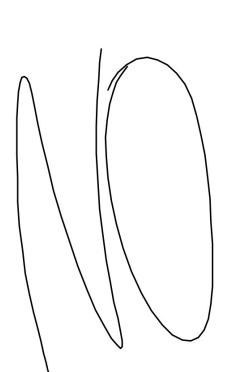
$$\frac{Sin A}{a} = \frac{Sin B}{Sin A} = \frac{C_1}{Sin A} = \frac{C_1}{S$$

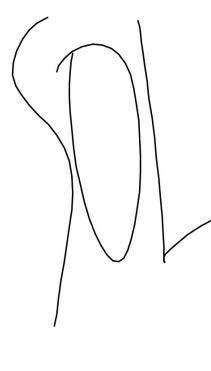
#### Ambiguous Cases: One solution

Now consider: Solve triangle  $\triangle ABC$  if  $\angle A=45^{\circ}$ ,  $\alpha=7\sqrt{2}$ , and b=7

# Ambiguous Cases: No solution

Now consider: Solve triangle  $\triangle ABC$  if  $\angle A=42^{\circ}$ ,  $\alpha=70$ , and b=122





General Guideline: Law of Sines

Law of Sines: 
$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$
  $= \frac{3 \sin C}{5 \sin A} = \frac{3 \cos C}{5 \cos A}$ 

<u>Two angles</u> and <u>one side</u> known: Only <u>1</u> possible outcome.

#### One angle and two sides known:

Case I- One outcome (angle measure of triangles cannot exceed 180)

Case II- Two possible outcomes

Case III- No possible outcome (sine of an angle cannot be greater than 1) ex.  $\sin A = 1.239$ no possible solution.

# **Homework Problems**

Solve each triangle using the Law of Sines.

11. 
$$\angle A = 50^{\circ}$$
,  $\angle B = 68^{\circ}$ ,  $c = 230$ 

# **Homework Problems**

Solve each triangle using the Law of Sines.

19. 
$$a = 20$$
,  $c = 45$ ,  $\angle A = 125^{\circ}$ 

# **Homework Problems**

Solve each triangle using the Law of Sines.

21. 
$$b = 25$$
,  $c = 30$ ,  $\angle B = 25^{\circ}$ 

# Homework 1/26

TB pg. 506 #1, 3, 5, 11, 15, 17, 19, 21, 23, 25