

Binomial Theorem

$$(a+b)^n = \binom{n}{0} a^n b^0 + \binom{n}{1} a^{n-1} b^1 + \binom{n}{2} a^{n-2} b^2 + \dots + \binom{n}{n} a^0 b^n$$

$$(a-b)^n = \dots - \dots + \dots - \dots$$

$$3) (n-m)^4 = \binom{4}{0} n^4 m^0 - \binom{4}{1} n^3 m^1 + \binom{4}{2} n^2 m^2 - \binom{4}{3} n^1 m^3$$

$$= n^4 - 4n^3m + 6n^2m^2 - 4nm^3 + m^4$$

$$+ \binom{4}{4} n^0 m^4$$

$$1) (y+2)^5$$

$$= \binom{5}{0} y^5 2^0 + \binom{5}{1} y^4 2^1 + \binom{5}{2} y^3 2^2 + \binom{5}{3} y^2 2^3 + \binom{5}{4} y^1 2^4 + \binom{5}{5} y^0 2^5$$

$$= y^5 + 5y^4 2 + 10y^3 4 + 10y^2 8 + 5y 16 + 32$$

$$\boxed{y^5 + 10y^4 + 40y^3 + 80y^2 + 80y + 32}$$

$$7) (y^4 - 3x)^5$$

$$= \binom{5}{0} (y^4)^5 (3x)^0 - \binom{5}{1} (y^4)^4 (3x)^1 + \binom{5}{2} (y^4)^3 (3x)^2 - \binom{5}{3} (y^4)^2 (3x)^3 + \binom{5}{4} (y^4)^1 (3x)^4$$

$$= y^{20} - 15y^{16}x + 90y^{12}x^2 - 270y^8x^3 + 405y^4x^4 - \binom{5}{5} (y^4)^0 (3x)^5$$

$- 243x^5$

13) $\binom{3}{1} (2y)^2 x^1$ 2nd term of $(2y+x)^3$

$$= 12y^2x$$

111th term of $(a+b)^{184}$

$$= \binom{184}{74} a^{90} b^{74}$$