

Objective

Students will...

 Be able to calculate the combination of numbers.

Combinations

A <u>combination</u> of r elements of a set is any subset of r elements from the set (without regard to order). If the set has n elements, then the number of combinations of r elements is denoted by: $\bigcirc \subset r \subseteq n$.

$$C(n,r) = {}_{n}C_{r} = {n \choose r}$$

We can read this as, "n choose r," denoting the number of ways to choose r elements of n elements. We can use any one of the three notations.

Example

For example, consider four elements, A, B, C, D. The combinations of these four elements taken three at a time, or in other words, the number of ways we can choose three of these four letters are...

ABC, ABD, ACD, BCD

Thus,
$$C(4,3) = {}_{4}C_{3} = {}_{4}{}_{3} \neq 4$$

Now, this problem wasn't too hard to explicitly write all of the possible combinations out and then simply count them. However, what if instead of just those 4 letters, we were considering the entire alphabet? That would be too tedious!

Combinations

This is why it's useful to have a general formula for finding combinations. This formula is relatively simple to derive using the counting principle, which we won't be learning until the probability section. For now,

$$C(n,r) = {}_{n}C_{r} = {n \choose r} = \frac{n!}{r!(n-r)!}$$
 where

$$n! = n \times (n-1) \times (n-2) \times \cdots \times 1$$

Ex.
$$\binom{4}{3} = \frac{4!}{3!(4-3)!} = \frac{4!}{3!1!} = \frac{4 \times 3 \times 2 \times 1}{(3 \times 2 \times 1)(1)} = \frac{24}{6} = 4$$

Example

Evaluate.
$$q! = \frac{q!}{4!(9.4)!} = \frac{q!}{4!5!} = \frac{9xxxxxx}{4!5!} = 126$$

b.
$$\binom{100}{3} = 100^{\frac{1}{3}} = 100^{\frac{1}{3}}$$

c.
$$\binom{90}{4} = \binom{7,595,190}{1,595,190}$$

Homework 4/23

TB pgs. 868 #13-20

13-20 ■ Evaluate the expression.

13.
$$\binom{6}{4}$$

14.
$$\binom{8}{3}$$

13.
$$\binom{6}{4}$$
 14. $\binom{8}{3}$ 15. $\binom{100}{98}$

16.
$$\binom{10}{5}$$

16.
$$\binom{10}{5}$$
 17. $\binom{3}{1}\binom{4}{2}$ 18. $\binom{5}{2}\binom{5}{3}$

18.
$$\binom{5}{2}\binom{5}{3}$$

19.
$$\binom{5}{0}$$
 + $\binom{5}{1}$ + $\binom{5}{2}$ + $\binom{5}{3}$ + $\binom{5}{4}$ + $\binom{5}{5}$

20.
$$\binom{5}{0} - \binom{5}{1} + \binom{5}{2} - \binom{5}{3} + \binom{5}{4} - \binom{5}{5}$$

$$\binom{6}{6}$$
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