Warm Up 9/9

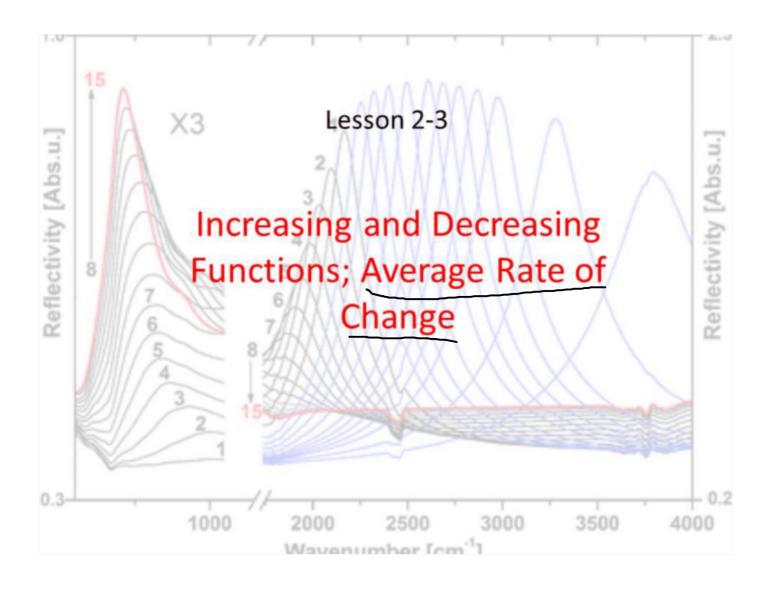
Find the slope of the line passing through the given points.

a.
$$(1,2)$$
, $(5,8)$ b. $(-1,3)$, $(0,2)$
 $M = \frac{rise}{run} = \frac{2ix}{2ix} = \frac{4i-3i}{2ix}$
 $\frac{4i-4i}{2ix-2i} = \frac{4i-4i}{2ix}$
 $\frac{4i-4i}{2ix-2i} = \frac{4i-4i}{2ix-2i}$
 $\frac{4i-4i}{2ix-2i} = \frac{4i-4i}{2ix-2i}$

c.
$$(0,0), (-11,7)$$

$$0-7 \left[-7 \right]$$

$$0-7 \left[-7 \right]$$



Objective

Students will...

- Be able to determine whether a function is increasing or decreasing algebraically and using graphs?
- Be able to compute the average rate of change, and understand its relationship to the secant line.

Increasing and Decreasing Functions

<u>Functions</u> are often used to model changing quantities. Thus, it's important to see and analyze where a function is <u>increasing</u> or <u>decreasing</u>.

A function, say f is...

Increasing on an interval I if $f(x_1) < f(x_2)$ whenever $x_1 < x_2$ in I. Decreasing on an interval I if $f(x_1) > f(x_2)$ whenever $x_1 < x_2$ in I.

In other words, when a bigger number is **inputted**, the **output** of an **increasing** function is greater, while the **output** of a decreasing function is smaller.

Examples

Determine whether the following functions are

increasing or decreasing at the given interval.

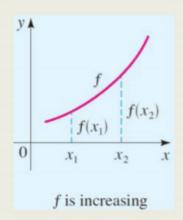
a.
$$f(x) = x + 2$$
; [1, 9]

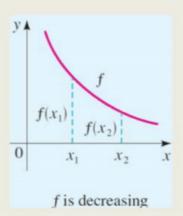
 $f(1) = 1 + 2 = 3$
 $f(q) = 9 + 2 = 11$
 $f(q) = 9 + 2 = 11$

b.
$$g(x) = \frac{3}{1+x^2}$$
; [-3,0]; [1,5]
 $f(-3) = \frac{3}{1+(-3)^2} = \frac{3}{10}$
 $f(0) = \frac{3}{1+0} = \frac{3}{10}$
 $f(5) = \frac{3}{1+25} = \frac{3}{10}$
 $f(5) = \frac{3}{1+25} = \frac{3}{10}$
 $f(5) = \frac{3}{1+25} = \frac{3}{10}$

Graphs of Increasing and Decreasing Functions

Increasing and decreasing functions can also be easily seen graphically.





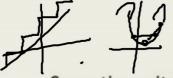
Thus, when viewing the graph from <u>left to right</u>, if the graph is rising the function is increasing, and vice-versa.

Examples

Determine the intervals on which the function W is increasing

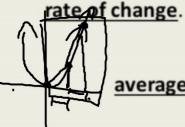
and on which it is decreasing, or neither. W (lb) ▲ 200 150 100 50 0 10 20 30 40 50 60 70 80 x (yr)

Inc:[0,25],[35,40] Dec:[40,50] Neille:[25,35],[50,80]



Average Rate of Change

Sometimes it is important to find how much a graph has increased or decreased within a certain interval. One of the most useful ways to analyze such change is calculating the average



average rate of change:
$$\frac{f(b)-f(a)}{b-a} = \frac{change in y}{change in x} = \frac{y_2-y_1}{x_2-x_1}$$

As you can see the average rate of change is really the slope of the line connecting the **two endpoints** of a given interval. This line connecting the two endpoints is known as the secant line.

Examples

For the function $f(x) = (x - 3)^3$, find the average rate of change between the following intervals: $f(a) = f(4) = (4-3)^2 - 1.$ a. [1,3] $f(b) = f(3) = (3-3)^3 = -8$ $f(a) = f(1) = (1-3)^3 = -8$

For the function $f(x) = (x-3)^3$, find the average rate of change between the interval [2,7]. f(b) = f(7) = 64f(a) = f(1) = -1

$$f(b)-f(a) = -1$$

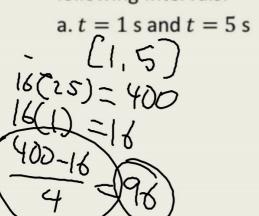
$$f(b)-f(a) = -1 \cdot 65$$

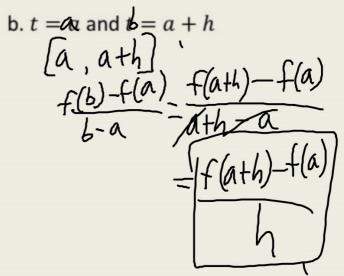
$$\frac{64-1}{5} \cdot 65$$

$$\frac{5}{5} \cdot a = 7-2 \cdot 13$$

Example

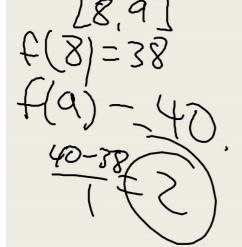
If an object is dropped from a tall building, then the distance it has fallen after t seconds is given by the function $d(t)=16t^2$. Find its average speed (average rate of change) over the following intervals:

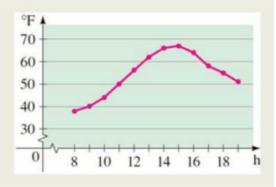




Using the graph of the function of temperature F(t) in given time t, find the average rate of temperature between the following times:

- a. 8am to 9am
- b. 1pm to 3pm
 - c. 4pm to 7pm







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